

Properties of logs Practice

$$1. \log_3(7x+3) = \log_3(5x+9)$$

$$2. \log_7(x-2) + \log_7(x+3) = \log_7 14$$

$$3. \log_2(5x+7) = 5$$

$$4. \ln(4x-1) = 3$$

$$5. \log_3(9x+2) = 4$$

$$6. \log_4 x + \log_4(x-12) = 3$$

$$7. \log_4(2x+1) = \log_4(x+2) - \log_4 3$$

$$8. \log_6(x+4) + \log_6(x-2) = \log_6(4x)$$

Properties of logs Practice

1. $\log_3(7x+3) = \log_3(5x+9)$

$$7x+3 = 5x+9$$

$$2x = 6$$

$$x = 3$$

2. $\log_7(x-2) + \log_7(x+3) = \log_7 14$

$$(x-2)(x+3) = 14$$

$$x^2 - x - 6 = 14$$

$$x^2 - x - 20 = 0$$

$$(x+4)(x-5) = 0$$

$$x = -4, 5 \quad \left(\begin{array}{l} -4 \text{ gives us a negative} \\ \log \text{ value so only } 5 \text{ works} \end{array} \right)$$

$$x = 5$$

3. $\log_2(5x+7) = 5$

$$5x+7 = 2^5$$

$$5x+7 = 32$$

$$5x+7 = 32$$

$$x = 5$$

4. $\ln(4x-1) = 3$

$$4x-1 = e^3$$

$$4x-1 \approx 20.085537$$

$$x \approx 5.271384$$

5. $\log_3(9x+2) = 4$

$$9x+2 = 3^4$$

$$9x+2 = 81$$

$$x = \frac{79}{9}$$

6. $\log_4 x + \log_4(x-12) = 3$

$$\log_4(x(x-12)) = 3$$

$$x(x-12) = 3$$

$$x^2 - 12x = 4^3$$

$$x^2 - 12x - 64 = 0$$

$$(x+4)(x-16) = 0$$

$$x = -4 \text{ or } 16$$

(-4 gives us a negative solution so only 16 works)

$$x = 16$$

7. $\log_4(2x+1) = \log_4(x+2) - \log_4 3$

$$\log_4(2x+1) = \log_4\left(\frac{x+2}{3}\right)$$

$$2x+1 = \frac{x+2}{3}$$

$$6x+3 = x+2$$

$$5x = -1$$

$$x = -\frac{1}{5}$$

(when substituted back into log equation a negative is produced)

no solution

8. $\log_6(x+4) + \log_6(x-2) = \log_6(4x)$

$$\log_6((x+4)(x-2)) = \log_6(4x)$$

$$x^2 + 2x - 8 = 4x$$

$$(x+2)(x-4) = 0$$

$$x = -2, 4$$

$$x = 4$$

(-2 gives us a negative solution so only 4 works)

Properties of logs

product rule: $\log_a(xy) = \log_a x + \log_a y$

$$\log_7 11x = \log_7 11 + \log_7 x$$

quotient rule: $\log_a\left(\frac{x}{y}\right) = \log_a x - \log_a y$

$$\log_6 \frac{2}{3} = \log_6 2 - \log_6 3$$

power rule: $\log_x y^p = p \log_x y$

$$\log_6 4^9 = 9 \log_6 4$$

change of base: $\log_x y = \frac{\log y}{\log x}$

$$\log_2 17 = \frac{\log 17}{\log 2} \approx 4.086$$

equality rule if $\log_a x = \log_a y$, then $x = y$

$$\log_8 (x+1) = \log_8 2x$$

$$x+1 = 2x$$

$$1 = x$$

EX $\log_3 x^2 y$

$$\log_3 x^2 + \log_3 y$$

$$2 \log_3 x + \log_3 y$$

EX $4 \log_7 (x+2) - 3 \log_7 (x-5)$

$$\frac{4 \log_7 (x+2)}{3 \log_7 (x-5)}$$

$$\frac{\log_7 (x+2)^4}{\log_7 (x-5)^3}$$